

# All-Electron Full-Potential Calculations at $\mathcal{O}(\text{ASA})$ Speed — A Fata Morgana?

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SFB 484, Teilprojekt D6

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# Outline

- 1 Background
- 2 Full-Potential ASW Method
- 3 Proof of Concept: Results

# Back in the 1930's ...

John C. Slater



*John C. Slater*

## Full Potential

$$v_{\sigma}(\mathbf{r}) : \begin{cases} \text{spherical symmetric near nuclei} \\ \text{flat outside the atomic cores} \end{cases}$$

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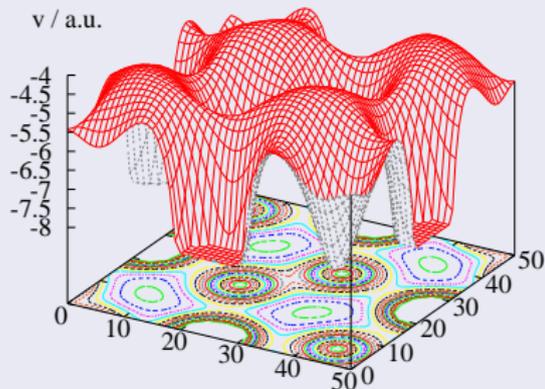
$$v_{\sigma}(\mathbf{r}) : \begin{cases} \text{spherical symmetric near nuclei} \\ \text{flat outside the atomic cores} \end{cases}$$

## Muffin-Tin Approximation

$$v_{\sigma}^{MT}(\mathbf{r}) = \begin{cases} \text{spherical symmetric in spheres} \\ \text{constant in interstitial region} \end{cases}$$

# Back in the 1930's ...

## Full Potential (FeS<sub>2</sub>)



## Muffin-Tin Potential



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## Muffin-Tin Approximation

distinguish:

- atomic regions
- remainder

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    - plane waves
    - spherical waves

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## Basis Functions

- matched partial waves
  - augmented plane waves (APWs)
  - „muffin-tin orbitals“ (MTOs), augmented spherical waves (ASWs)

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## Wave Function

expand in basis functions

- expansion coefficients from variational principle

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## Core States

all-electron methods

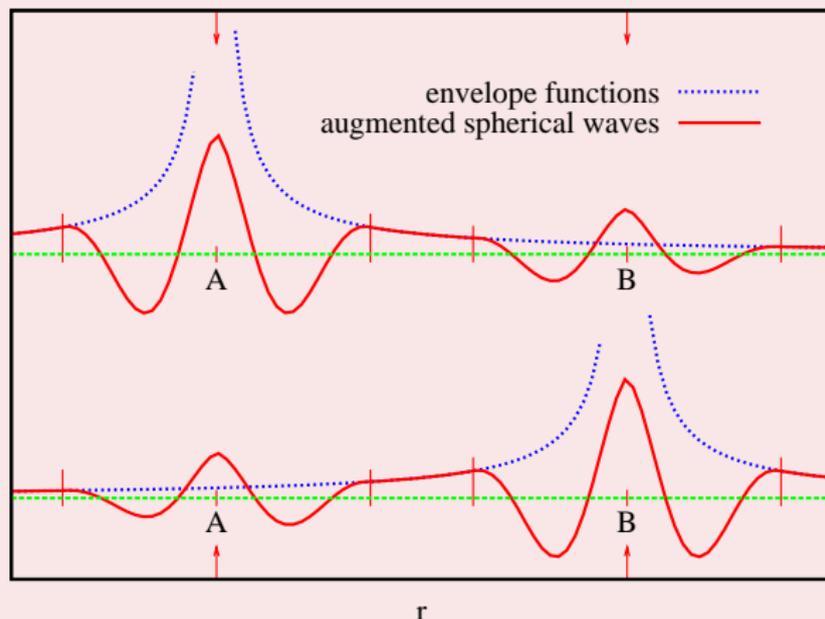
- fully included
- orthogonal to partial waves

## Basis Functions

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  - augmented plane waves (APWs)
  - „muffin-tin orbitals“ (MTOs), augmented spherical waves (ASWs)
- used to describe valence states

# Back in the 1930's ...

## Augmented Spherical Waves



# Back in the 1970's ...

Ole K. Andersen



## “Linear Methods in Band Theory”

- energy dependence of basis functions almost linear  $\rightarrow$  linearize  $(\varphi, \dot{\varphi})$ 
  - huge increase in computat. efficiency!

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## Linear Augmented Plane Wave (LAPW)

- muffin-tin approximation
- easy to implement good!
- full-potential at a low price
  - basis functions from muffin-tin potential
  - wave functions from full potential
  - example: Wien2k
- large basis set ( $\approx 100$  pw's/atom) bad!

# Back in the 1970's ...

## Ole K. Andersen



## Linear Muffin-Tin Orbital (LMTO)

- based on spherical waves
  - does not require crystalline periodicity
  - natural interpretation of results
- difficult to implement **bad!**
- **full-potential extension extremely difficult**
- muffin-tin approximation (?)
  - finite interstitial region
  - large basis set:  
two functions per  $s$ -,  $p$ -,  $d$ -state
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    - **interstitial region formally removed**
    - **only numerical functions in spheres**
  - **minimal basis set ( $s$ ,  $p$ ,  $d$ )**
    - **very high computational efficiency**  
→  $\mathcal{O}(\text{ASA})$  speed!!!
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  - **systematic error in total energy** bad!

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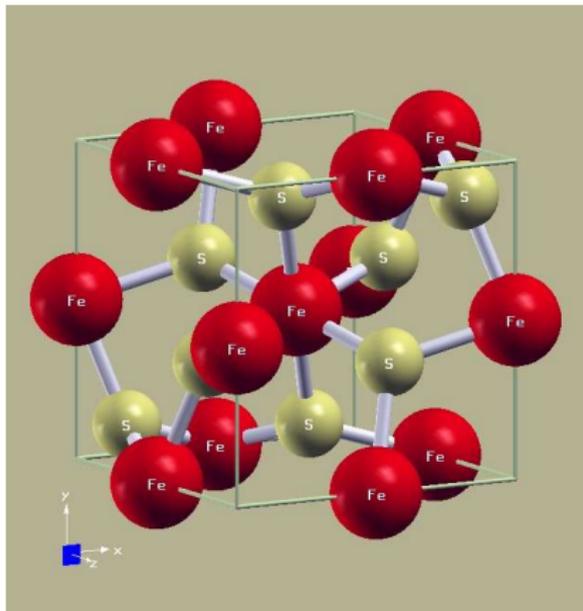
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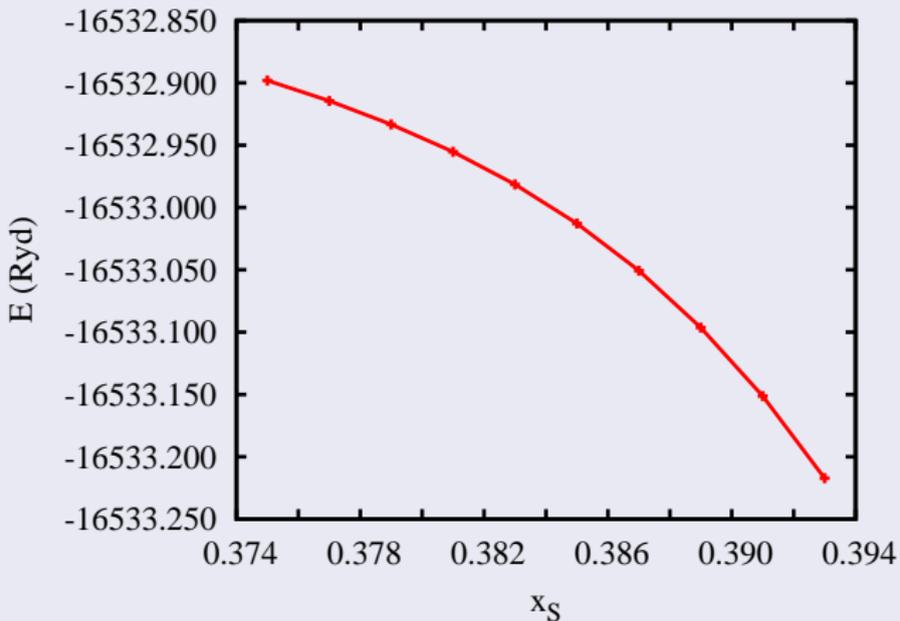


## Pyrite

- $Pa\bar{3} (T_h^6)$
- $a = 5.4160 \text{ \AA}$
- “NaCl structure” sublattices occupied by
  - iron atoms
  - sulfur pairs
- sulfur pairs  $\parallel \langle 111 \rangle$  axes
- $x_S = 0.38484$
- rotated  $\text{FeS}_6$  octahedra

# FeS<sub>2</sub>: Structure Optimization

## ASW Version 2.2



# Towards a Full-Potential Spherical-Wave Method

## Conclusions

- ASA (space-filling atomic spheres)
  - $\mathcal{O}(\text{ASA})$  speed
  - systematic error in total energy
- non-overlapping muffin-tin spheres
  - prerequisite for accurate total energies
  - larger basis set  $\rightarrow$  inefficient

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## Requirements

- restore interstitial region
  - go to non-overlapping muffin-tin spheres
  - go beyond constant-potential approximation
- inside muffin-tin spheres
  - non-spherical contributions

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- interstitial quantities expanded in **plane waves**
  - straightforward to implement
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- interstitial quantities expanded in **spherical waves**
  - elegant, no periodicity required
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## Characteristics

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  - different linearization scheme
  - different interstitial energy
  - different implementations

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0th Generation (Williams, Kübler, Gelatt, 1970s)

PRB **19**, 6094 (1979)

# ASW Method

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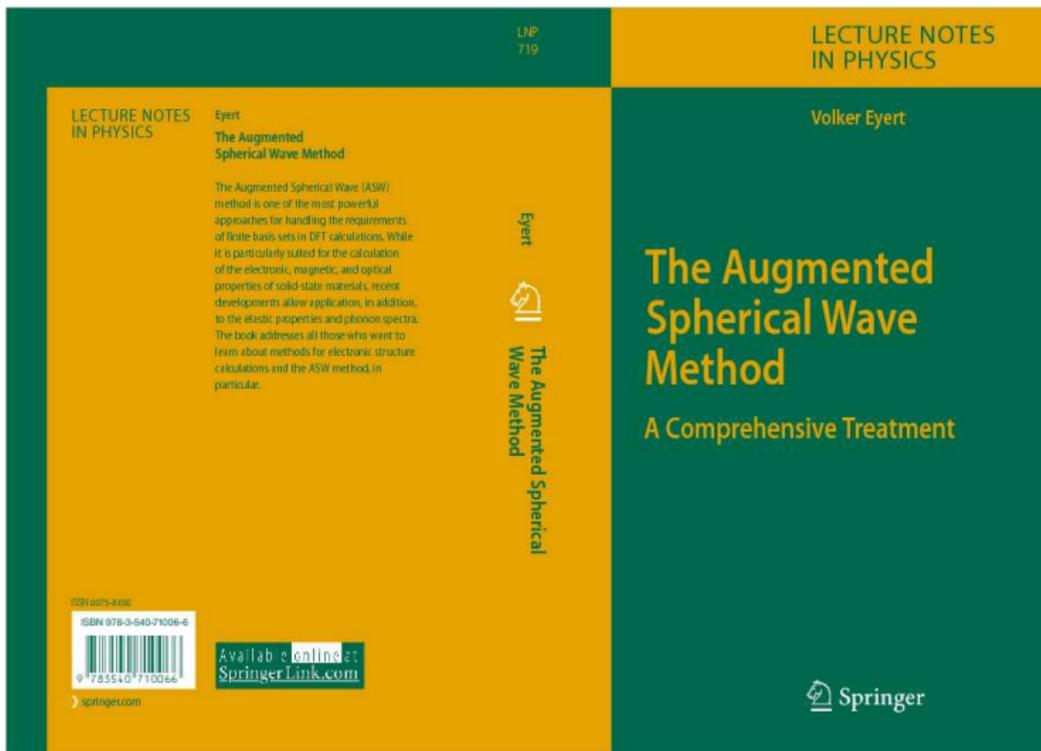
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## 1st Generation (VE, 1990s)

IJQC 77, 1007 (2000)

- completely new, monolithic implementation
- new algorithms → improved accuracy, numerical stability
- much improved functionality, usability, and portability
- all LDA-parametrizations, most GGA-schemes
- many new interpretative tools
- still based on atomic-sphere approximation

# ASW Method: Further Reading



# Outline

- 1 Background
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# Basic Principles

## Steps to be Taken

- **remove total energy error** due to overlap of atomic spheres
  - reintroduce non-overlapping muffin-tin spheres
  - restore interstitial region

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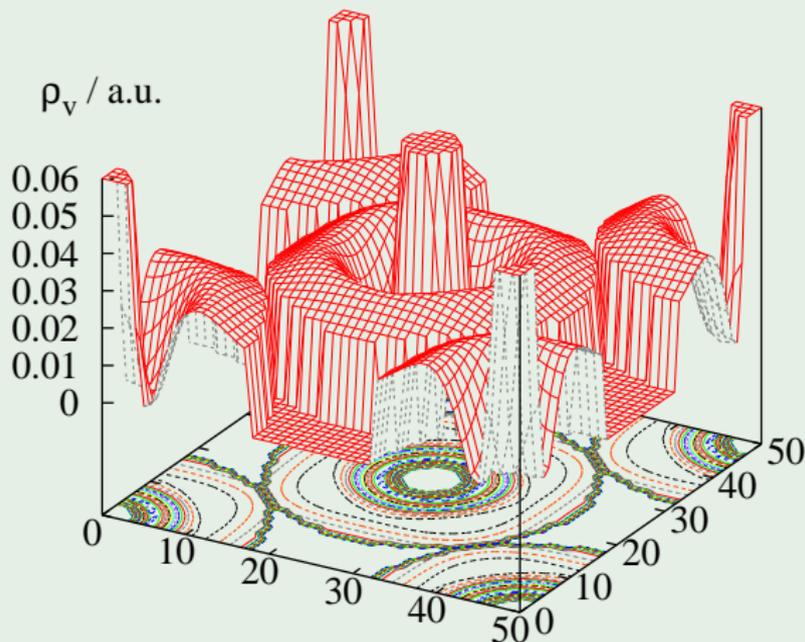
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- find representation of **products of the basis functions**
  - inside muffin-tin spheres
    - **use spherical-harmonics expansions**
  - in the interstitial region
    - **no exact spherical-wave representation available!**

# From Wave Functions to Electron Density

## Density inside MT-Spheres

(A)



# From Wave Functions to Electron Density

## Products of Basis Functions in Interstitial Region

$$\rho^l(\mathbf{r}) = \sum_n d_n F_n(\mathbf{r})$$

$$\int d^3\mathbf{r} F_{n'}^*(\mathbf{r}) \rho^l(\mathbf{r}) = \sum_n d_n \int d^3\mathbf{r} F_{n'}^*(\mathbf{r}) F_n(\mathbf{r})$$

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- $F_n(\mathbf{r})$ : plane waves
  - integrals exact
  - inefficient
  - Weyrich 1988, Blöchl 1989, VE 1991, Savrasov 1992, Methfessel 2000

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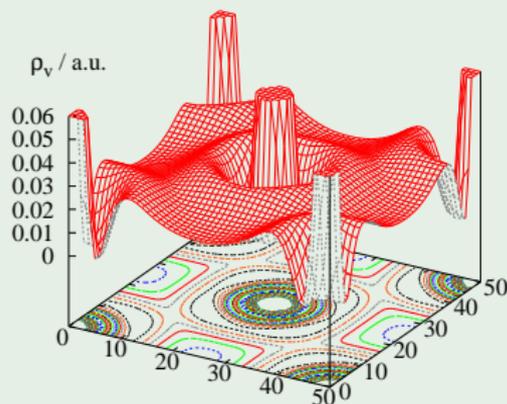
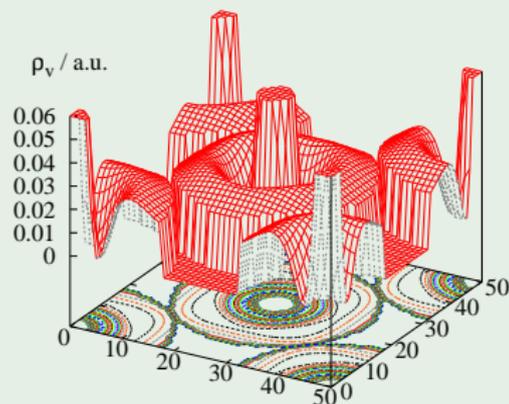
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  - Methfessel 1988:  
match values and slopes at MT-sphere surfaces

# From Wave Functions to Electron Density

## Density from Value/Slope Matching at MT-Radii (A)

(A)





# From Electron Density to Full Potential

## Inside Muffin-Tin Spheres

- density, Hartree-potential and xc-potential numerically

## Interstitial Region

- density from value/slope matching
- Hartree-potential analytically
- xc-potential from value/slope matching

# From Full Potential to Basis Functions

## Previous Approaches

- project full potential to **muffin-tin potential**
- construct basis functions from **muffin-tin potential**
- **no minimal basis set!** (large basis set!)

## Present Approach

- project full potential to **ASA potential**
- construct basis functions from **ASA potential**
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## Ole K. Andersen

- ASA geometry used for basis functions  
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# Implementation

## 2nd Generation ASW (VE, 2000s)

- based on 1st generation code
- full-potential ASW method
  - electron densities, spin densities
  - electric field gradients
  - elastic properties, phonon spectra
- optical properties
  - based on linear-response theory
  - direct calculation of  $\Re\sigma$  and  $\Im\sigma$
  - no Kramers-Kronig relations needed
- LDA+U method
  - all „flavours“ for double-counting terms (AMF, FLL, DFT)

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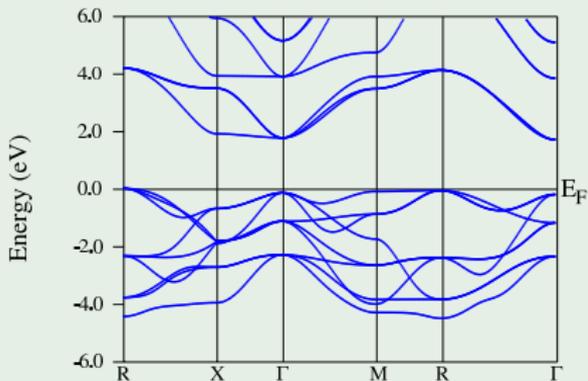
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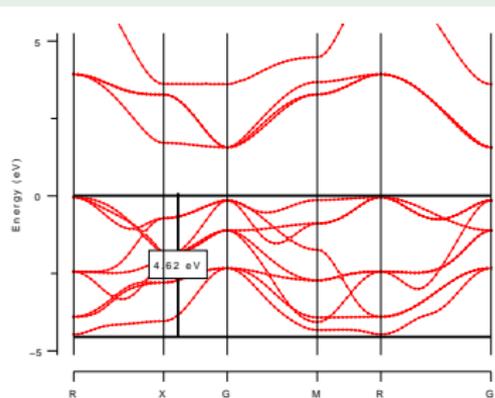


# Electronic Structure of BaTiO<sub>3</sub>

Wien2k

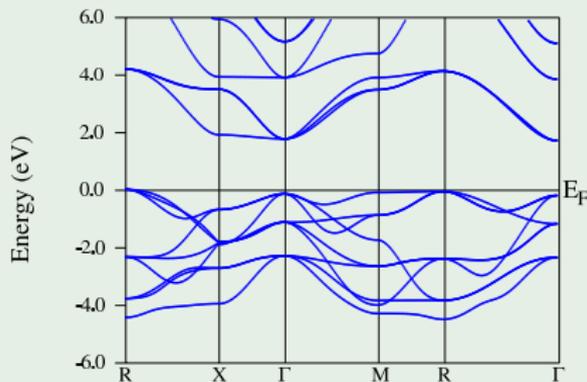


VASP

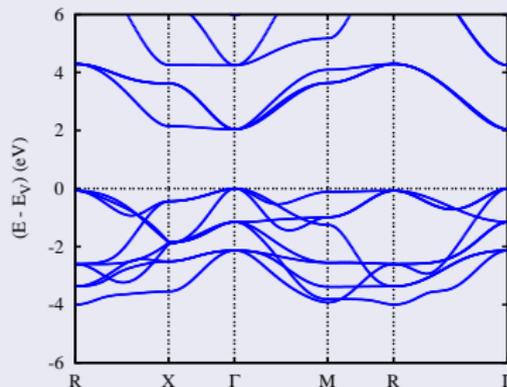


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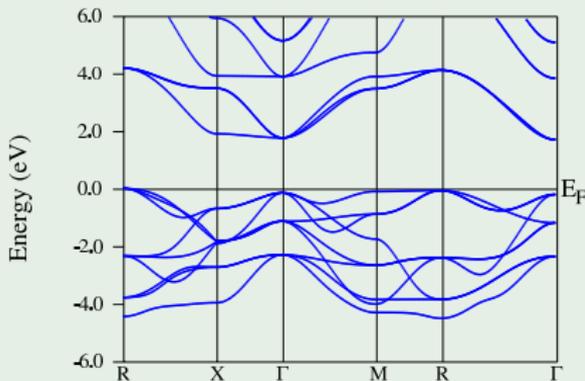


ASW Version 2.2

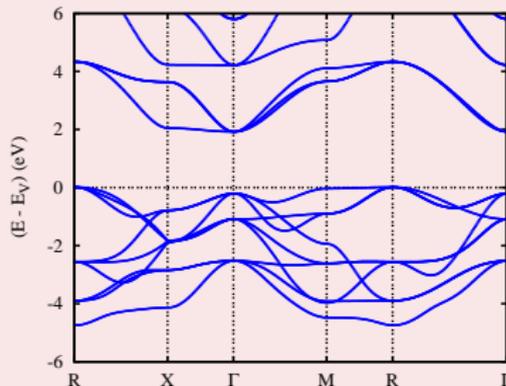


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FPASW Version 2.3

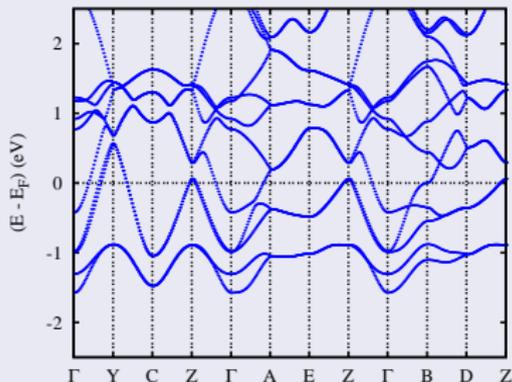


New!

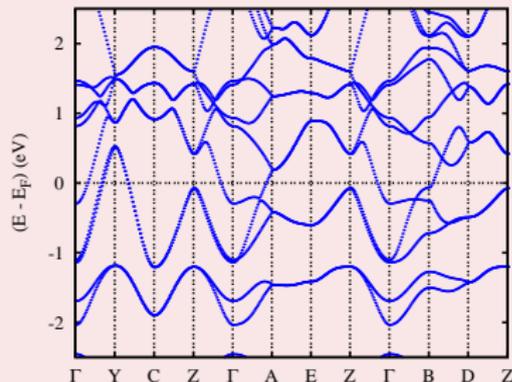
- much better agreement with other full-potential codes (valence-band width, valence states at M-point)

# Fermi Surface of $\text{MoO}_2$

ASW Version 1.9



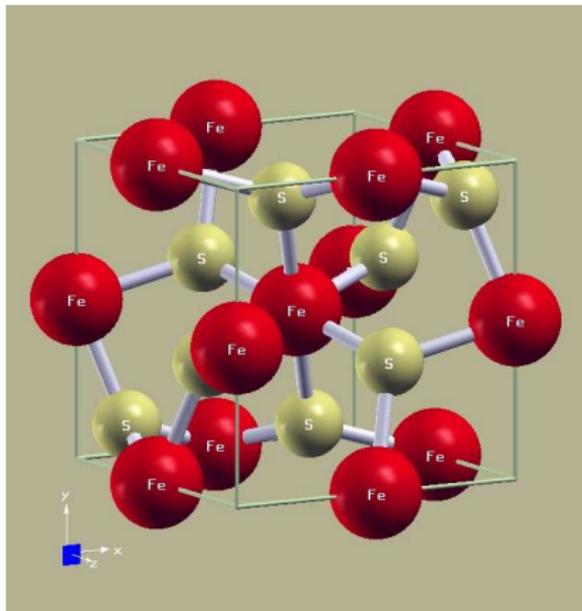
FPASW Version 2.3



New!

- no hole pocket near Z-point
- much better agreement with ARPES, de Haas-van Alphen

# Iron Pyrite: $\text{FeS}_2$

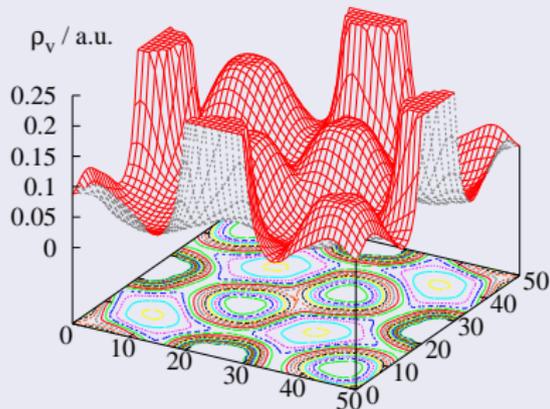


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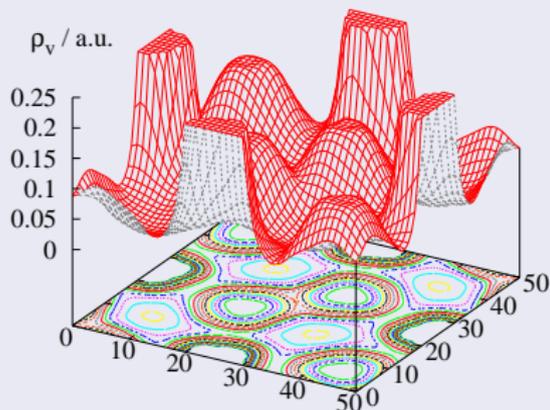
# FeS<sub>2</sub>: Density and Laplacian

## Valence Electron Density

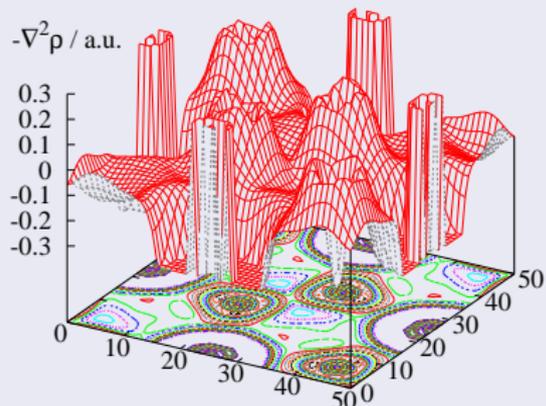


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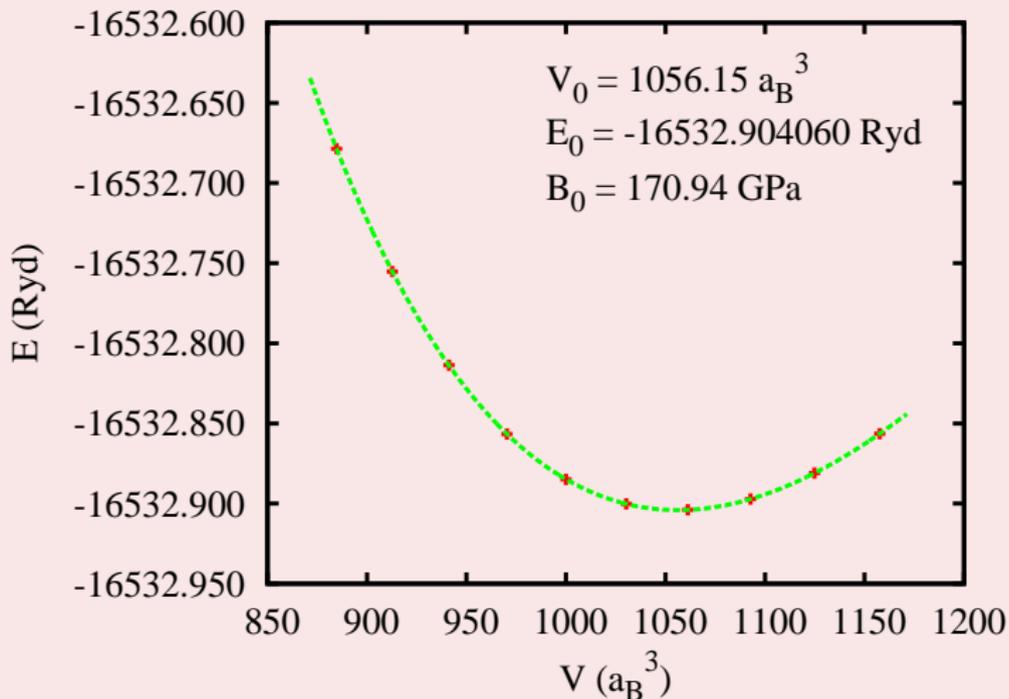
## Laplacian of Electron Density



New!

- topological analysis (Bader analysis)

# FeS<sub>2</sub>: Equilibrium Volume and Bulk Modulus



# FeS<sub>2</sub>: Equilibrium Volume and Bulk Modulus

## Lattice Constant

10.28	NCPP	Zeng and Holzwarth '94
10.02	FPLO	Opahle <i>et al.</i> '99
10.17	CRYSTAL98	Muscat <i>et al.</i> '02
9.92	CASTEP	Muscat <i>et al.</i> '02
10.18	FPASW	present work
10.23	exp.	Finklea <i>et al.</i> '76
10.22	exp.	Will <i>et al.</i> '84
10.23	exp.	Stevens <i>et al.</i> '91

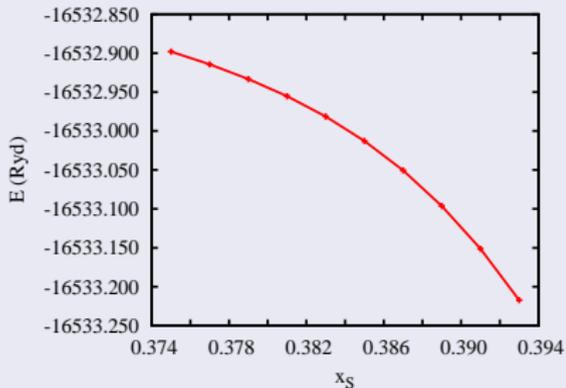
# FeS<sub>2</sub>: Equilibrium Volume and Bulk Modulus

## Bulk Modulus

187	LMTO	Nguyen-Manh <i>et al.</i> '98
185	FPLO	Opahle <i>et al.</i> '99
209	CRYSTAL98	Muscat <i>et al.</i> '02
208	CASTEP	Muscat <i>et al.</i> '02
<b>171</b>	<b>FPASW</b>	<b>present work</b>
148	exp.	Drickamer <i>et al.</i> '66
118	exp.	Will <i>et al.</i> '84
215	exp.	Chattopadhyay and von Schnering '85
157	exp.	Fujii <i>et al.</i> '86
143	exp.	Jephcoat and Olson '87
162	exp.	Ahrens and Jeanloz '87
145	exp.	Blachnik <i>et al.</i> '98

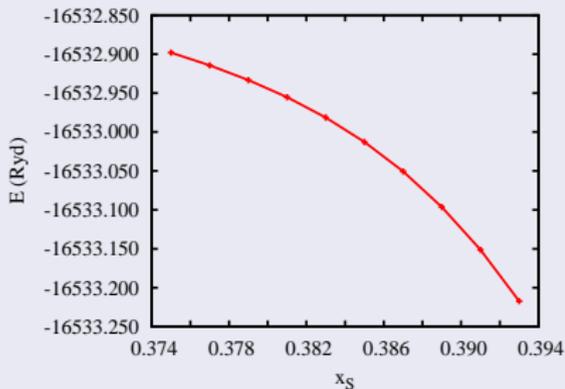
# FeS<sub>2</sub>: Structure Optimization

## ASW Version 2.2

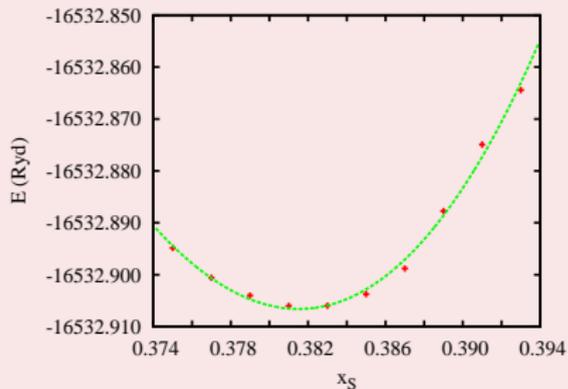


# FeS<sub>2</sub>: Structure Optimization

## ASW Version 2.2



## FPASW Version 2.3



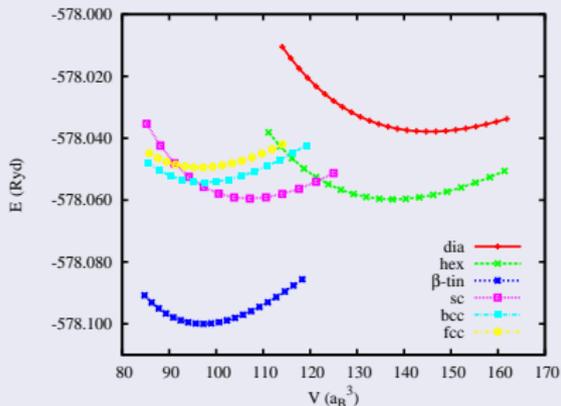
# FeS<sub>2</sub>: Structure Optimization

## Sulfur Position

0.378	NCPP	Zeng and Holzwarth '94
0.377	FPLO	Opahle <i>et al.</i> '99
0.378	CRYSTAL98	Muscat <i>et al.</i> '02
0.382	CASTEP	Muscat <i>et al.</i> '02
<b>0.382</b>	<b>FPASW</b>	<b>present work</b>
0.386	exp.	Finklea <i>et al.</i> '76
0.386	exp.	Will <i>et al.</i> '84
0.385	exp.	Stevens <i>et al.</i> '91

# Phase Stability in Silicon

## ASW Version 2.2

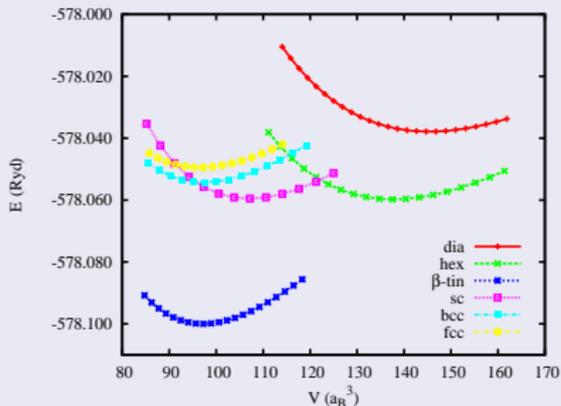


Bad

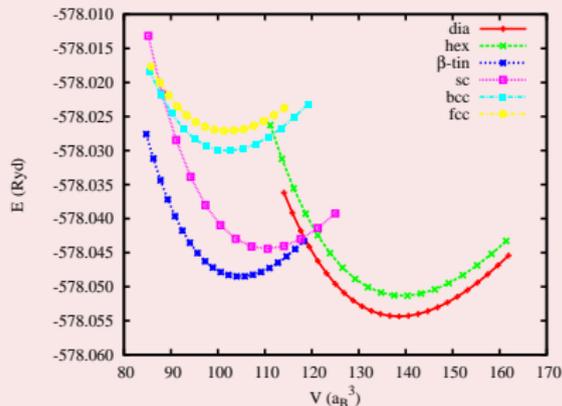
- $\beta$ -tin structure most stable # nature (diamond structure)

# Phase Stability in Silicon

## ASW Version 2.2



## FPASW Version 2.4

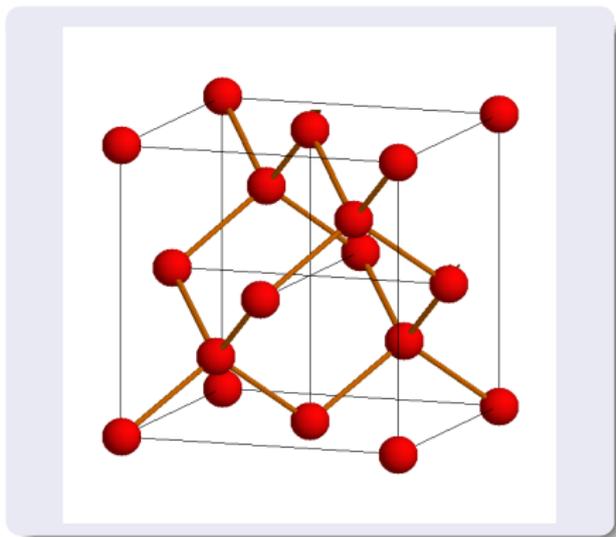
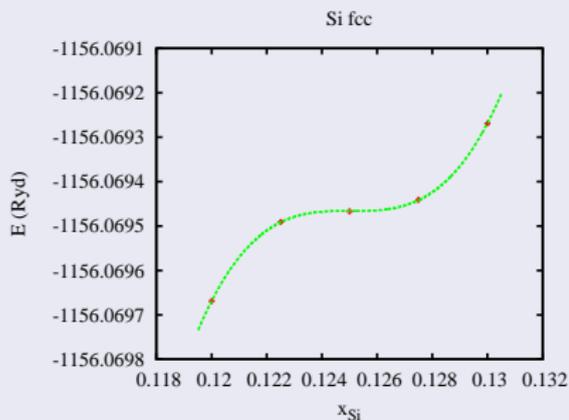


## New!

- diamond structure most stable
- pressure induced phase transition to  $\beta$ -tin structure

# LTO( $\Gamma$ )-Phonon in Silicon

## ASW Version 2.2

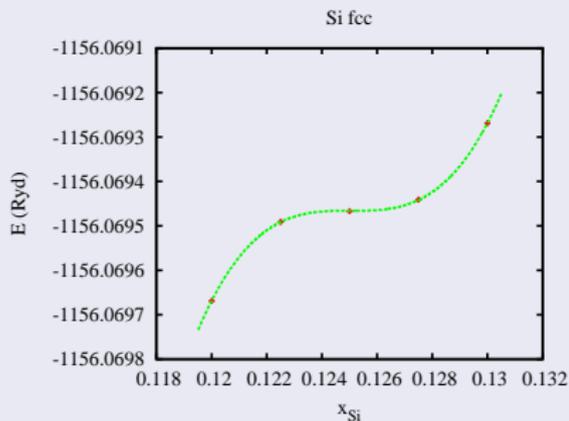


Bad

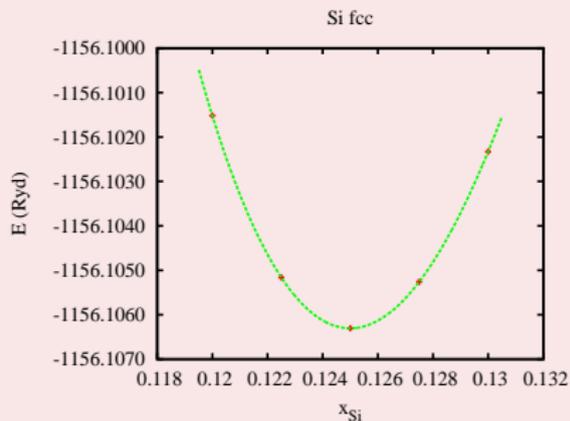
- no stable Si position # nature

# LTO( $\Gamma$ )-Phonon in Silicon

## ASW Version 2.2



## FPASW Version 2.4



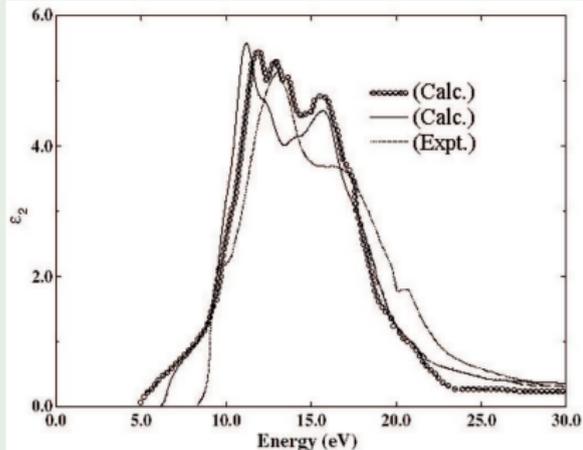
New!

- phonon frequency:  $f_{calc} = 15.26$  THz ( $f_{exp} = 15.53$  THz)

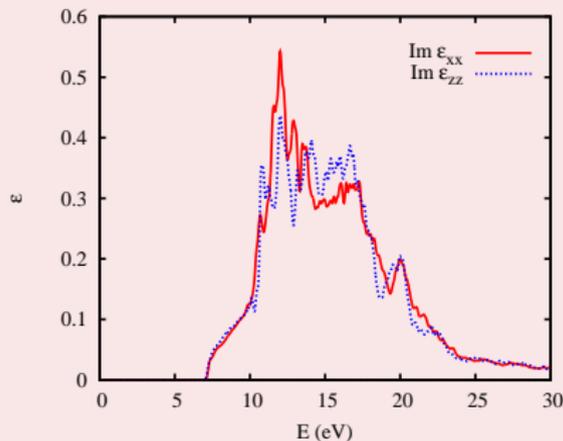
# Dielectric Functions of Corundum

## Imaginary Part

FLAPW, Hosseini *et al.*, 2005  
FPLMTO, Ahuja *et al.*, 2004



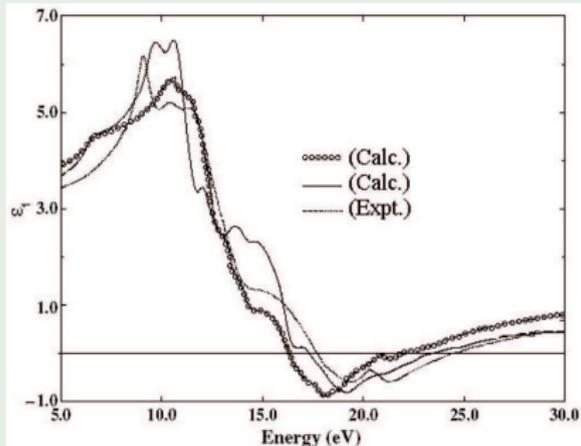
FPASW



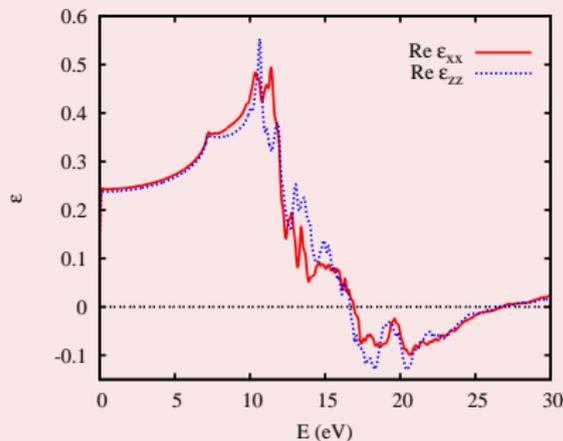
# Dielectric Functions of Corundum

## Real Part

FLAPW, Hosseini *et al.*, 2005  
FPLMTO, Ahuja *et al.*, 2004

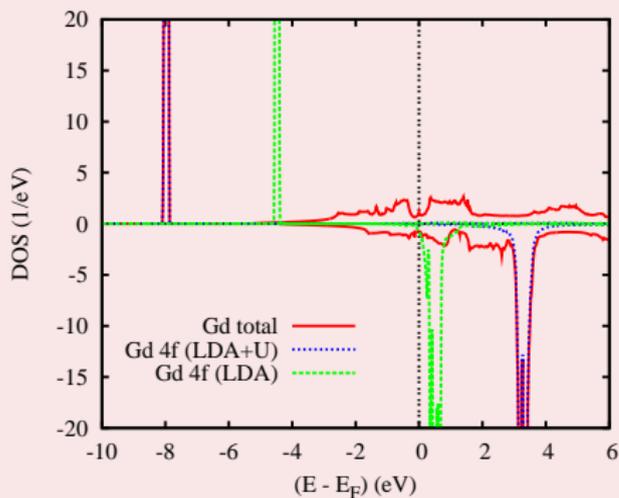


## FPASW



# LDA+U-Calculations for Gadolinium

## DOS of ferromagnetic Gd



## Energetics

	$E_{AF} - E_{FE}$
LDA	-1.601
LDA+U	8.425

(in mRyd/atom)

# Summary

## Full-Potential ASW Method

(Versions 2.3/2.4)

- ASA Geometry used for Basis Functions
- MT Geometry used for Density and Potential
- Accurate Total Energies
- $\mathcal{O}(\text{ASA})$  Speed!
- Optical Properties implemented
- LDA+U-Method implemented

## What's Next?

- Forces? Automated Structure Optimization?
- Improved Treatment of Exchange (EXX) and Correlations (LDA+DMFT, EXX+DMFT)?

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# Acknowledgments

Stuttgart

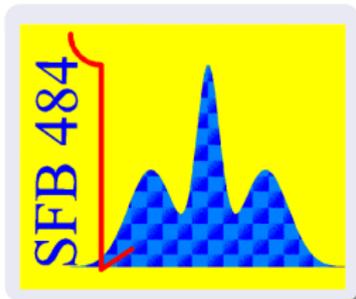
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## Thank You for Your Attention!